



A High-level Overview of MAESTRO Mapping Directives and Cost Model

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Outline

- **Mapping Representation: A data-centric representation**
 - Computation and Data Space
 - Data-centric Directives
 - Deep-dive Example: Eyeriss-like Dataflow

 **MAESTRO Cost Model – High Level Overview**

Source Code Structure

Cost-model/include/

[base](#): Base class definitions

[tools](#): Misc. helper classes (output file generation, etc.)

[user-api](#): API class (code level APIs)

[dataflow-specification-language](#): Directive syntax definition, parser, etc.

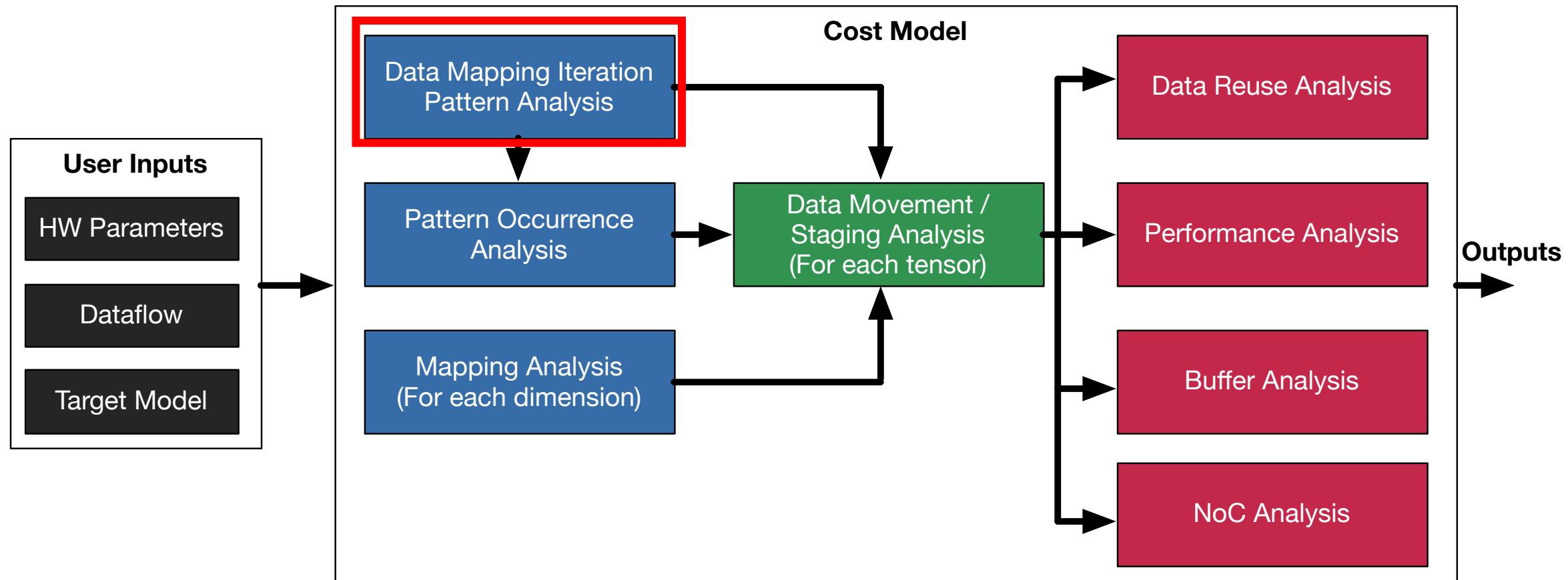
[abstract-hardware-model](#): Hardware performance and cost models

[dataflow-analysis](#): Data reuse analysis

[cost-analysis](#): Compute the costs using data reuse analysis results

[design-space-exploration](#): (Will be renamed) Contains base HW cost information

Cost Model Overview



Mapping Iteration Pattern Analysis

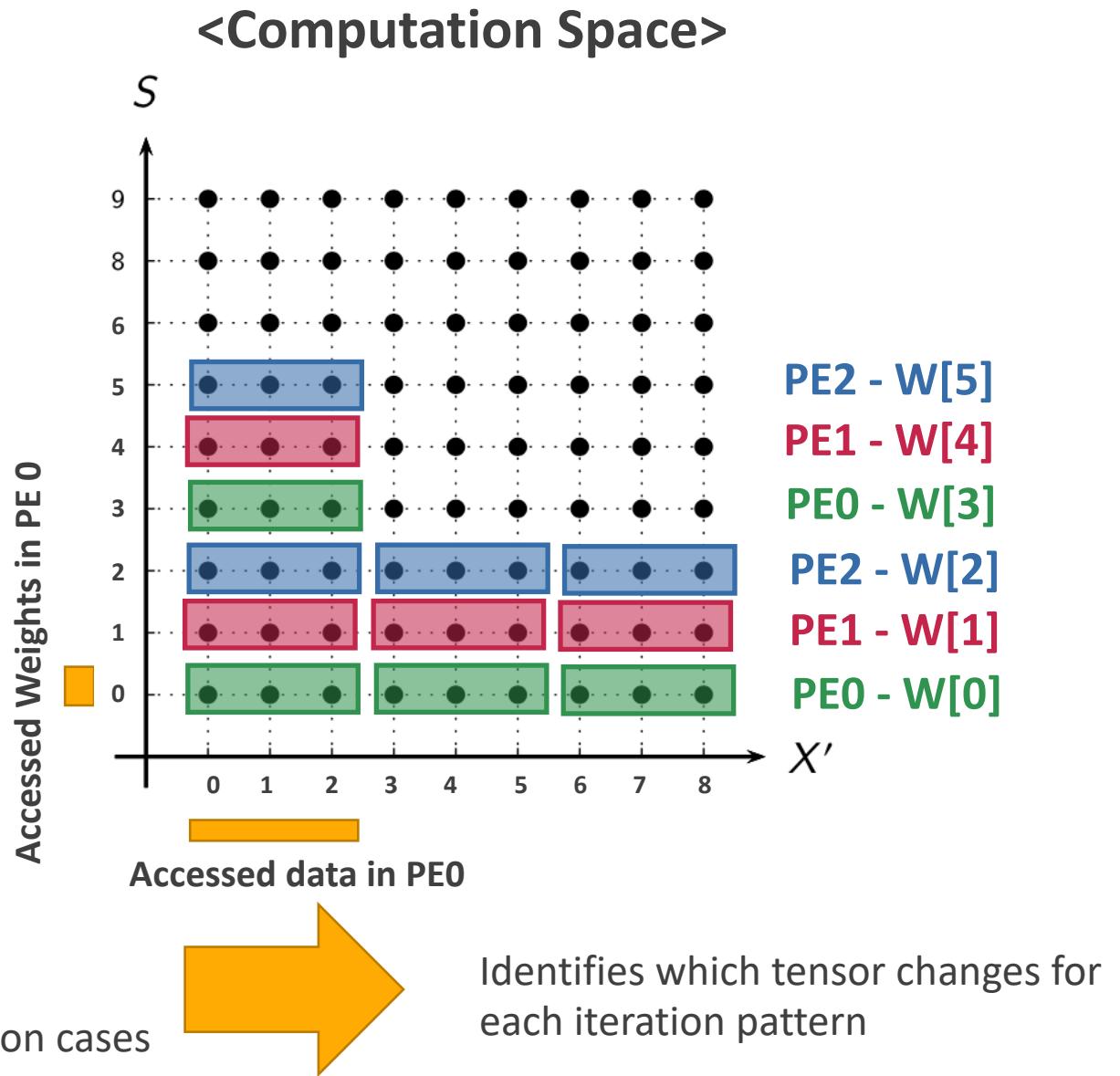
SpatialMap(Sz=1, Ofs=1) S
TemporalMap(Sz=3, Ofs=3) X
Cluster(Sz=3)
TemporalMap(Sz=1, Ofs=1) S
SpatialMap(Sz=1, Ofs=1) X

Filter: Init Filter: Init
Input: Init Input: Steady

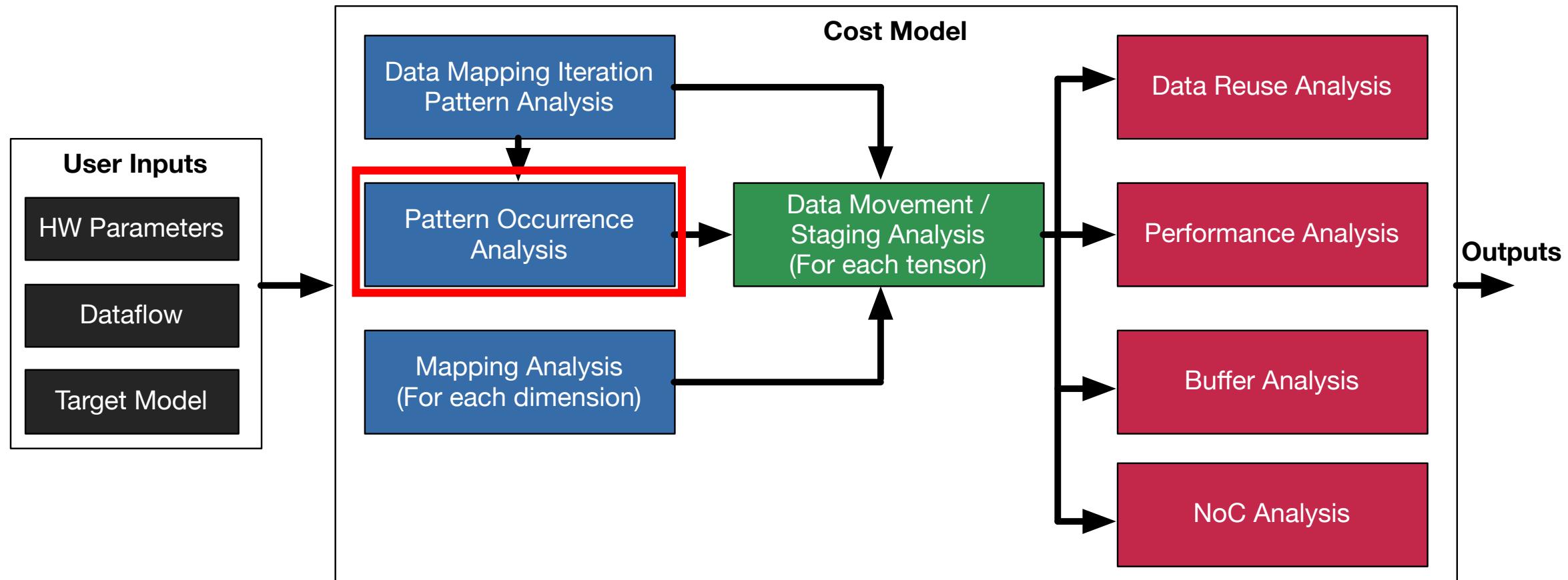
Filter: Steady
Input: Init

Mapping iteration Status = {Init, Steady, Edge}

Analysis is performed on each dimension in higher dimension cases



Cost Model Overview



Mapping Iteration Pattern Count Analysis

<Computation Space>

SpatialMap(Sz=1, Ofs=1) S
TemporalMap(Sz=3, Ofs=3) X
Cluster(Sz=3)
TemporalMap(Sz=1, Ofs=1) S
SpatialMap(Sz=1, Ofs=1) X

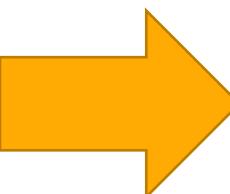
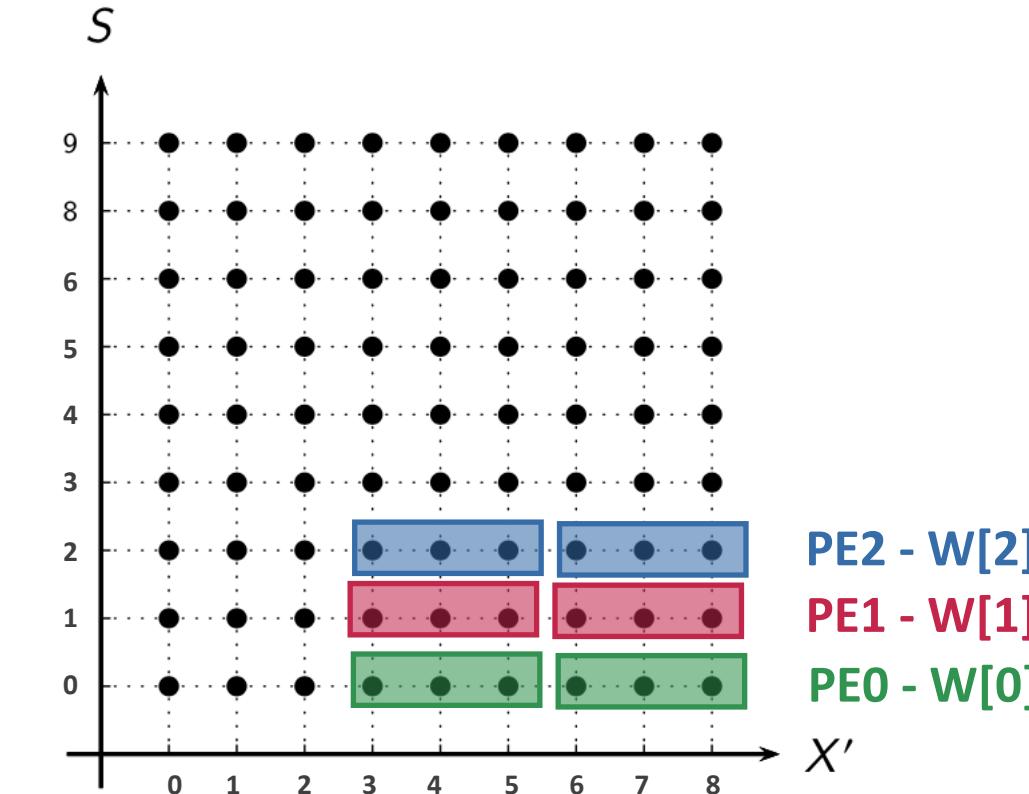
Filter: Init
Input: Steady

Input

Dimension(X') / MapSz(X') = 3
Subtract init case; 3-1 = 2

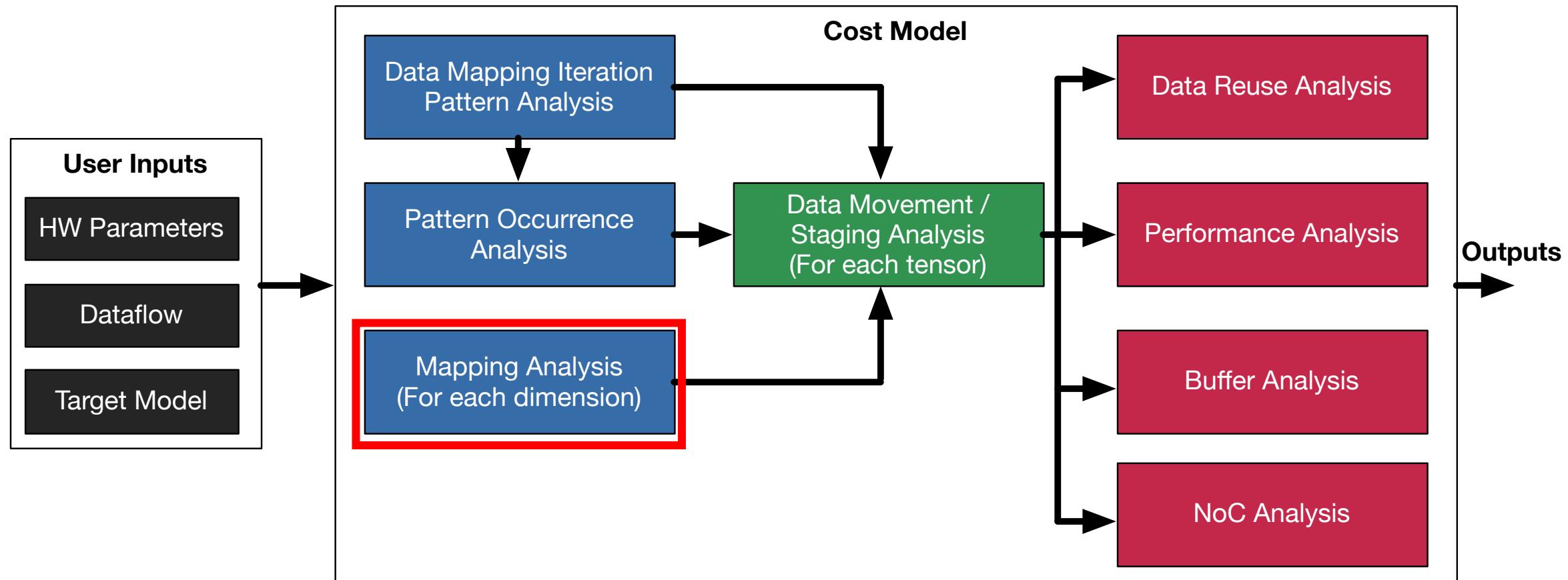
Filter

Init case = 1

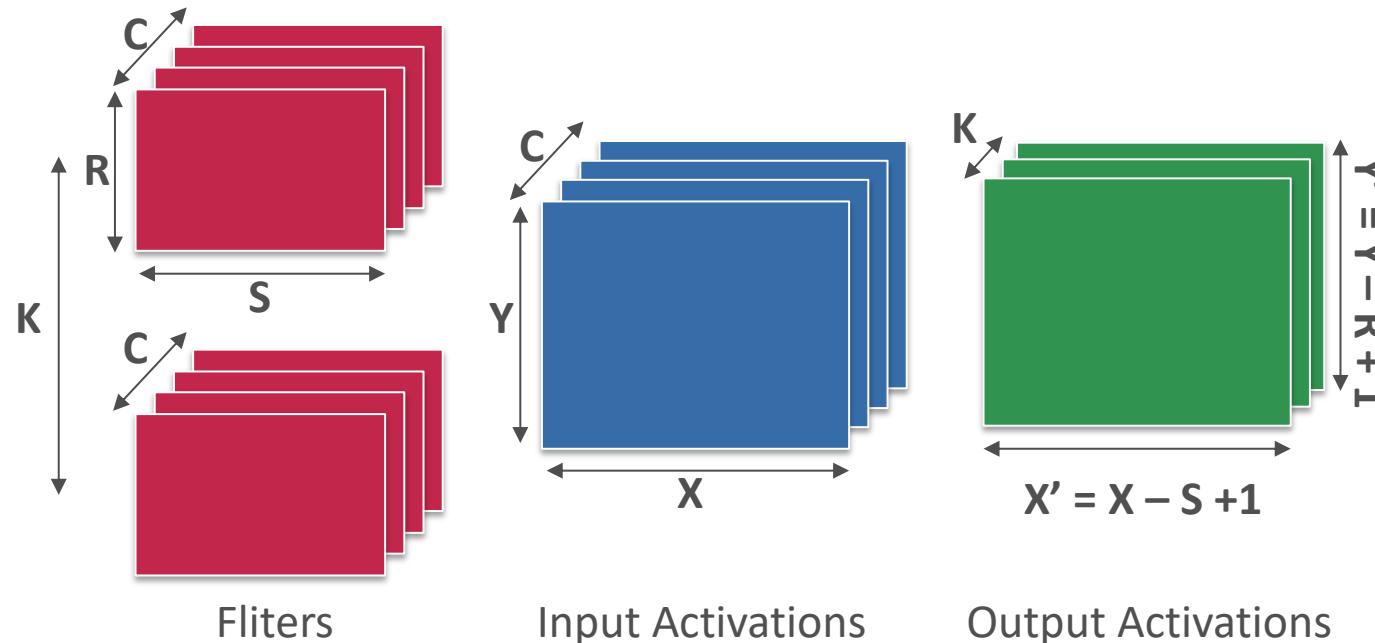


2x1 = twice

Cost Model Overview



Mapping Analysis - Convention



Data Dimensions (Loop Variables)

- K/C : Input/output Channel
- Y/X : Input Height/Width
- R/S : Filter Height/Width
- N : Batch

Variable Data class	Output Channel (K)	Input Channel (C)	Filter Row (R)	Filter Column (S)	Input Row (Y)	Input Column (X)
Output Activation	X		X	X	X	X
Input Activation		X			X	X
Filter Weights	X	X	X	X		

* Output row(Y') = $Y - R + 1$, Output column(X') = $X - S + 1$

Mapping Analysis

Variable Data class	Output Channel (K)	Input Channel (C)	Filter Row (R)	Filter Column (S)	Input Row (Y)	Input Column (X)
Output Activation	X		X	X	X	X
Input Activation		X			X	X
Filter Weights	X	X	X	X		

* Output row(Y') = Y-R+1, Output column(X') = X-S+1

TemporalMap (1, 1) N

TemporalMap (2, 2) K

TemporalMap (2, 2) C

TemporalMap (3, 3) R

TemporalMap (3, 3) S

TemporalMap (3, 1) Y

SpatialMap (3, 1) X

How many *weight pixels* do we map on each PE?

$$2 \times 2 \times 3 \times 3 = 36 \text{ pixels}$$

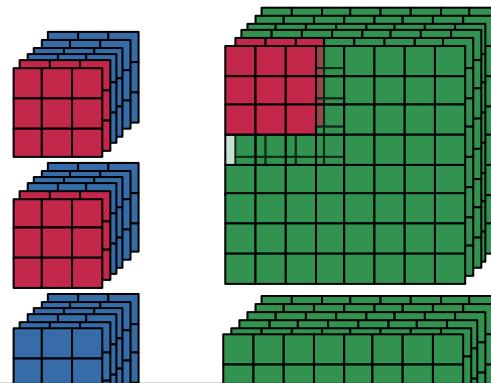
Syntax

TemporalMap (MapSz, Ofs) Var
SpatialMap (MapSz, Ofs) Var

Mapping Analysis

TemporalMap (MapSz, Ofs) Var
SpatialMap (MapSz, Ofs) Var

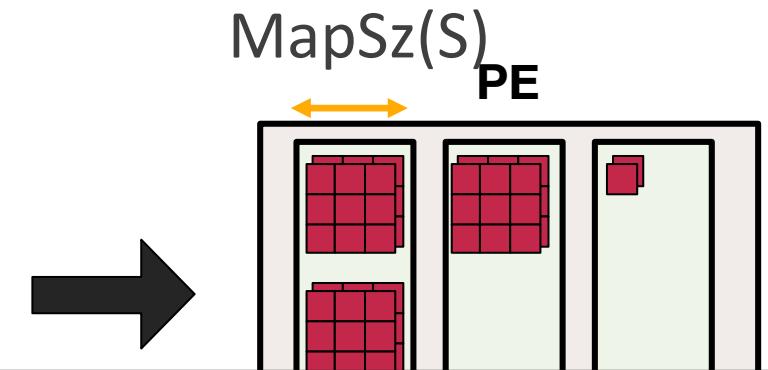
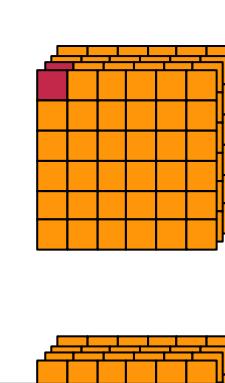
TemporalMap (1, 1) N



TemporalMap (2, 2) K

TemporalMap (2, 2) C

TemporalMap (3, 3) R



When a mapped “Volume” moves, do we have overlaps over time?

TemporalMap (3, 1) Y



How many? (How much data reuse do we have?)

$$\text{MV(Weight)} = \text{MapSz}(K) \times \text{MapSz}(C) \times \text{MapSz}(R) \times \text{MapSz}(S)$$
$$\text{MV(Initial)} = M(S(N)) \times M(S(C)) \times M(S(R)) \times M(S(Y))$$

How many over time? And, how many among PEs at the same time?

MV: Mapped Volume

Extending to 6D case

//MV: Mapped volume

MV[Weights] = $M(K) \times M(C) \times M(R) \times M(S)$

MV[Inputs] = $M(C) \times M(Y) \times M(X)$

MV[Outputs] = $M(K) \times M(Y') \times M(X')$

//MSUV: Mapped spatially unique volume

MSUV[Weights] = $GetSpUSz(K) \times GetSpUSz(C) \times GetSpUSz(Y) \times GetSpUSz(X)$

MSUV[Inputs] = $GetSpUSz(C) \times GetSpUSz(Y) \times GetSpUSz(X)$

MSUV[Outputs] = $GetSpUSz(K) \times GetSpUSz(C) \times GetSpUSz(Y') \times GetSpUSz(X')$

//MTUV: Mapped temporally unique volume

MTUV[Weights] = $TU(K) \times TU(C) \times TU(R) \times TU(S)$

MTUV[Inputs] = $TU(C) \times TU(Y) \times TU(X)$

MTUV[Outputs] = $TU(K) \times TU(C) \times TU(Y') \times TU(X')$

Analyze the number of unique/reused pixels in each data class for each mapping iteration pattern

MSTUV[Weights] = $GetSTpUSz(K) \times GetSTpUSz(C) \times GetSTpUSz(R) \times GetSTpUSz(S)$

MSTUV[Inputs] = $GetSTpUSz(C) \times GetSTpUSz(Y) \times GetSTpUSz(X)$

MSTUV[Outputs] = $GetSTpUSz(K) \times GetSTpUSz(C) \times GetSTpUSz(Y') \times GetSTpUSz(X')$

* $GetSpUSz(V) = (V.\text{pragma}.\text{class} == \text{TemporalMap})? M(V) : SU(V);$

* $GetSTpUSz(V) = (V.\text{pragma}.\text{class} == \text{SpatialMap})? SU(V) : TU(V);$

Terms

TU: Temporally unique values

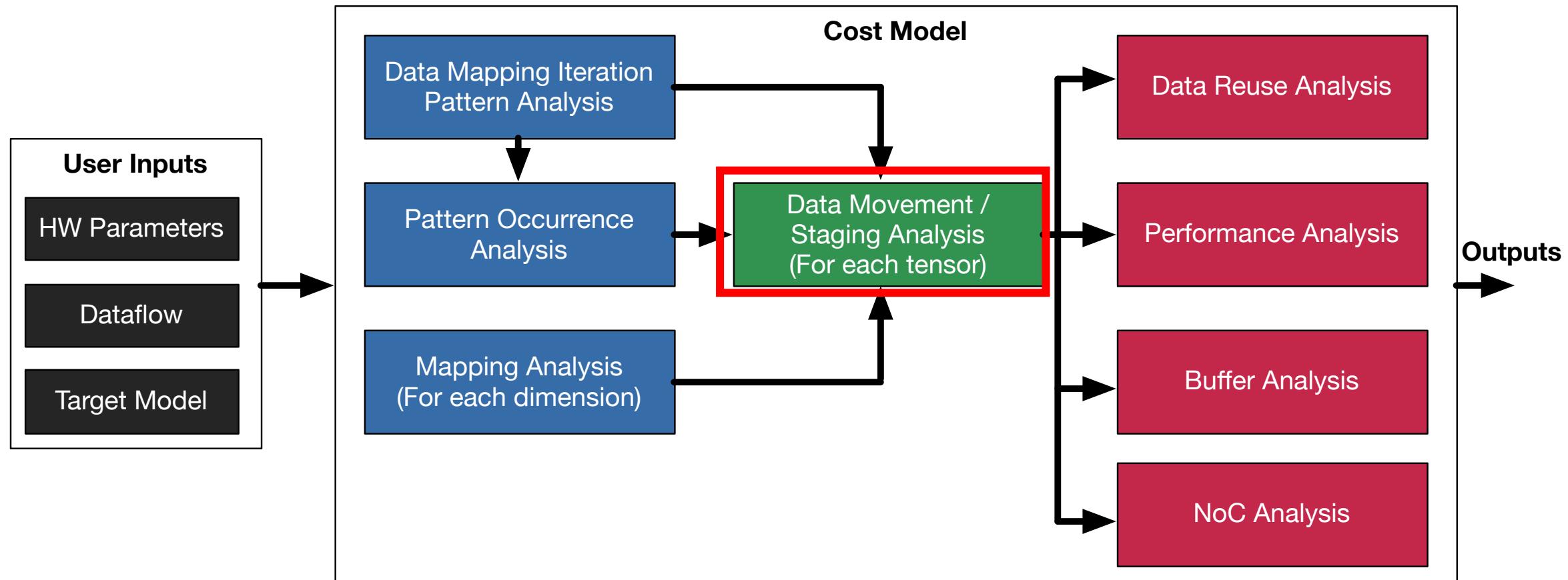
SU: Spatially unique values

SPUSz: Spatially unique values

TUV: Temporally unique volume

SUV: Spatially unique volume

Cost Model Overview



Intuition for Rest of Cost Model

- Iteration pattern analysis provides information regarding
 - Which tensor changes in between two mappings
 - How many times is each one repeated
- For details, please see the source code and web page (<http://maestro.ece.gatech.edu>)
 - Overall, how many data points are mapped over each PE
 - If a tensor changes, how many data points are reused

Combining information we can extract..

- 1) Amount of data to be transferred from global buffer to PE array
- 2) Amount of computation to be done in each mapping
- ...